# ANALYSIS OF PLANE STRAIN ROLLING RIGID PLASTTIC MATERIALS USING FINITE ELEMENT METHOD 

Saad Theeyab Faris<br>Assistant Professor, College of Engineering, University of Diyala<br>dr-saadthf2014@yahoo.com<br>(Received: 23/3/2014; Accepted: 18/8/2014)


#### Abstract

In this research the rigid plastic material is applied to steady and nonsteady state strip rolling .Stresses and strains distribution in steady state plane strip rolling under the condition of constant of friction are calculated for work hardening and nonhardening materials .In order to attain a comprehensive understanding of the underlying process details, to check and select semi analytical models, highly sophisticated numerical approaches, based on the method of finite elements (F.E.M), have been performed by utilizing the non-linear capabilities of both ANSYS-11 Standard and Explicit., Analytical models, (with different reduction of areas) validated against each other and calibrated with real process data, are essential to determine proper rolling setups of aluminum (according to roller diameter, distance between rollers and rolling pressure). The calculated distribution of roll pressure exhibits, a peak at the entry which does not appear in the analysis by the slab method. The transverse direction (TD) rotation angle which increases an accurate elongation control system was built, which is based on precise mathematical process models for the prediction of rolling pressure, velocity and forward slip. To improve the quality of the rolled product rolling provides a slight reduction in thickness, thereby eliminating the yield point elongation focusing on the surface elements which exhibit a compressive stress. The TD rotation angle in the rolled specimens are very small and permanent deformation due to the rolling process, these result of completed shapes are in a good agreement with the experimental ones for aluminum strip .


Keywords: Cold Roll Forming, Rigid Plastic Metal Forming, Finite Element Analysis.

## Notation

A Area pf roll-strip interface
F External force
g Small positive constant
$\mathrm{m} \quad$ Total number of elements
$\mathrm{N} \quad$ Total number of nodes
P Roll pressure
$P_{r} \quad$ normal component of force
R Roll radius
r Reduction in thickness
to Initial thickness
V Volume of element
v Velocity of surface where external force is prescribed
$\tau_{f} \quad$ Frictional shear stress at roll-strip interface
$\varphi \quad$ Functional
$\omega \quad$ Angular velocity
RD Rolling direction
ND Normal direction
TD Transverse direction

## 1. INTRODUCTION:

In the analysis of strip rolling, the slab method based on a simplified equilibrium of force was first suggested by ${ }^{(1,2,3)}$ which derived approximate solutions of equilibrium equation by employing various assumptions this method is widely applied in industry for designing and controlling rolling mills. However, the method is not good enough to carry out accurate predictions of pressure distribution and inhomogeneous deformation. Cold roll formed parts have become increasing important in recent years, and made their way into whole new sectors like the automobile industry. The reasons for this include the introduction of new kinds of materials and improved shaping tool design and their large variety of applications. Cold roll forming is seen as a highly productive process for manufacturing Aluminum sections through continuous shaping of sheet Aluminum by driven rolls ${ }^{(4)}$. Particular advantages of this process are the virtually unlimited shape variety of profile cross sections, and the strain hardening of the material resulting from the shaping process, which can be turned to good advantage if toll design is done properly. These are the benefits. But there are also drawbacks like, in many instances, the time-consuming design and production of roll tools, installation, startup and try-outs of tool sets, or undesirable internal strain or deformation of the end-product ${ }^{(5)}$.

In rolling process the metal is subjected to high compressive stresses as a result of the friction between the rolls and the metal surface. In the analysis of strip rolling, the slab method based on a simplified equilibrium of force was first suggested by ${ }^{(6)}$ which derived approximate solutions of the equilibrium equation, by employing various assumptions. The method is widely applied in industry for designing and controlling rolling mills, however, the method is not good enough to carry out accurate predictions of pressure distribution and inhomogeneous deformation. although some other methods such as the slip-line field method ${ }^{(7,8)}$ and the upper bound method have been proposed for the analysis of rolling ,their industrial application is limited .the finite element method is expected to be used for
simulating metal forming process because realistic boundary conditions and materials properties can be taken into account .however ,the rolling process is not easily treated even by the finite element method because of the difficulties associated with the boundary condition in that the strip is driven by the frictional force over the roll surface and no velocity is given by any plane. Most past studies in relation to the finite element method have assumed no slipping between the strip and the roll surfaces to provide a simple velocity boundary condition in plane - strain rolling .Employing this assumption ${ }^{(9,10)}$.The elastic -plastic F.E analysis of the rolling process is also carried out from an initial nonsteady state to a steady by using the infinitesimal deformation theory to include more realistic frictional conditions assumed a constant coefficient of friction and analyzed planestrain and rigid plastic finite element methods ${ }^{(11)}$. The above reasons lead to the subject of analysis and optimization software (ANSYS-11), presenting a whole lot of potential to remedy the situation. To get cold roll forming up and going with all its efficiency, there is a need to apply methods as early as the profile and tool design phase that can play a major role in improving the quality of the rolled section.

## 1.1- The goal

The goal of this research is analyze the cold roll forming process of rigid plastic material using (ANSYS-11) software program computes the theoretical (elastic and plastic) strain values on the material during forming as a function of influencing variable like profile cross section geometry, material gauge, roll configuration or diameter. In this way it is able to indicate where the material might be overstressed, This fast simulation program enables to run through a whole series of different shaping variants and to correct the draft flower or number of shaping stations and toll dimensions as necessary before starting the actual detailing work or even production of the roll tools, This is time saving and it reduces the risk of having to rework the roll tool later at start up or even having to make them a fresh in many cases, the major of poor profile quality is residual local deformation of the sheet metal (internal strain) produced by elongation during roll forming in addition to the theoretical figures for such elongation on the top and under side of the metal. Predicts how the figures are distributed over the cross section. Strain even though the majority of profile cross sections that are produced are in fact stressed over their entire cross section during roll forming.

## 2- TEORY

## 2.1- Basic equations

The total deformation gradient (F) can be decomposed into two components ${ }^{(9)}$.
$F=\frac{\partial x}{\partial X}=F^{\bullet} F^{p}$
The velocity gradient $(\mathrm{L})$ is evaluated from the deformation gradient by
$L=\frac{\partial v}{\partial x}=F F^{-1}=L^{\cdot}+L^{p} \quad---------(2 a)$
$L^{*}=F^{*} F^{*-1}$
Where $v$ is the velocity in the deformed configuration, F expresses a time derivative of $\mathrm{F}, \mathrm{L}^{*}$ is the contribution of the elastic and lattice rotation to $L$ and $L^{*}$ the plastic contribution. Considering referencing [13] it is assumed that the strip is slightly compressible in plastic deformation so the yield criterion for plane -strain deformation is given by

$$
\begin{equation*}
\sigma=\sqrt{\frac{1}{2}}\left\{\left(\sigma_{x}-\sigma_{y}\right)^{2}+\left(\sigma_{y}-\sigma_{z}\right)^{2}+\left(\sigma_{z}-\sigma_{x}\right)^{2}+6 \tau_{x y}^{2}\right\}+g \sigma m^{2} \tag{3}
\end{equation*}
$$

Where $g$ is a small positive constant, the stress is calculated from the strain rate as follows:-

$$
\begin{align*}
& \sigma_{x}=\sigma^{\prime}\left\{\frac{2}{3} \varepsilon^{\prime} x_{x}+\left(\frac{1}{g}-\frac{2}{9}\right) \varepsilon^{\prime}{ }_{v}\right\} / \varepsilon^{\prime},  \tag{4}\\
& \sigma_{y}=\sigma^{\prime}\left\{\frac{2}{3} \varepsilon^{\prime}{ }_{y}+\left(\frac{1}{g}-\frac{2}{9}\right) \varepsilon^{\prime}{ }_{v}\right\} / \varepsilon^{\prime},  \tag{5}\\
& \sigma_{z}=\sigma^{\prime}\left(\frac{1}{g}-\frac{2}{9}\right) \varepsilon_{v}{ }^{\prime} / \varepsilon^{\prime}{ }_{y} \\
& \tau_{x y}=\sigma^{\prime} \gamma_{x y}^{\prime} / 3 \varepsilon \\
& \left.\varepsilon^{\prime}=\sqrt{\left(\frac{4}{9}\right.}\left(\varepsilon^{,{ }^{2}}{ }_{x}-\varepsilon^{\prime}{ }_{x} \varepsilon^{\prime}{ }_{y}+\varepsilon^{\prime}{ }^{2}{ }_{y}+\frac{3}{4} \gamma^{\prime}{ }_{x y}\right)+\frac{1}{g} \varepsilon^{\varepsilon^{\prime}{ }_{v}}\right) .
\end{align*}
$$

Consider that a rigid - plastic strip is deformed between rigid rolls under plane -strain condition with tensile stress applied at the front and tail ends, as shown in fig (1).the strip is driven by frictional shear stress distributing over the roll surface. The functional defined in the reference [9] is given as follows for the plastically deforming strip divided into elements.

$$
\begin{aligned}
& \phi=\sum_{i=1}^{m 1}\left(\sigma^{\prime} \varepsilon^{\prime} V\right)_{i}+\sum_{i=1}^{m 2}\left(\tau_{f} A \Delta v\right)_{i}-\sum_{i=1}^{m 3}\left(F v^{\prime}\right)_{i}----(9) \\
& \left.\left.\Delta v=\sqrt{\left(\frac { 1 } { 2 } \left(\left\{\left(u_{h}+R \omega \sin \alpha_{h}\right)^{2}\right.\right.\right.}+\left(u_{h-} R \omega \cos \alpha_{h}\right)^{2}+\left(u_{h+1}+R \omega \sin \alpha_{h+1}\right)^{2}+\left(u_{h-1}-R \omega \cos \alpha_{h+1}\right)^{2}\right\}\right)----10 z
\end{aligned}
$$

Where V is the volume of element A the area of roll -strip interface, $\Delta \mathrm{v}$ the relative velocity at the interface, $F$ the external force and $v$ the velocity of the surface where the external force is prescribed .the correct solution renders the functional a minimum, and when the value g is as small as $0.01-0.0001$; the velocity field which minimizes $\Phi$ gives only slight volumetric strain rate $\dot{\varepsilon}_{v}$ and the volume is kept almost constant.

At only one point along the surface of contact between the roll and the sheet, two forces act on the metal. a radial force Pr and a tangential frictional force F , If the surface
velocity of the roll Vr equal to the velocity of the sheet, this point is called neutral point or no slip point (point N in figure (2). Between the entrance plane ( xx ) and the neutral point the sheet is moving slower than the roll surface and the tangential friction force F act in the direction to draw the metal in to the roll. On the exit side (y) of the neutral point, the sheet moves faster than the roll surface, the direction of the frictional force is then reversed and opposes the delivery of the sheet from the rolls. Pr is the radial force with a vertical component Pr (rolling load - the load with which the rolls press against the metal. The specific roll pressure P is the rolling load divided by the contact area. The distribution of roll pressure along the arc of contact shows that the pressure rises to maximum at the neutral point and then falls off. The pressure distribution does not come to a sharp peak at the neutral which indicates that the neutral point is not really a line on the roll surface but an area. Figure (3).

## 2.2- Geometry

The geometry of the initial mesh (Figure 4) is an estimation of the expected steady state geometry. The mesh movement is kept fixed in rolling direction. The material flows through the mesh in rolling direction which results in an inflow and an outflow boundary. The mesh follows the free surface perpendicular to the rolling direction. Internal nodes are repositioned in order to preserve a sufficient element quality. Due to symmetry only half specimen was modeled. The steady state rolling continuous rolling of strip without front and back tension is analyzed. The process geometries and working condition are in as follows in table (1) and the symmetric boundary conditions were applied to the mid-plane of the specimen. The reductions in thickness vary from $10 \%$ to $60 \%$. The effects of two types of initial evolution have been investigated. Contact elements are used to describe the contact between the strip and the tools. These elements are based on a penalty formulation, the tools are modeled rigid and instead of a force, the motion of the tools is prescribed. This means that the deformation and the mutual displacement of the tools is not taken into account. In practice this is an important issue as it affect the final dimensions of the sheet .The material which has been used for the experiments is Aluminum 6061. This material is modeled with an elastic - plastic material model with a Von-Misses flow rule. The hardening is described by the stress - strain curve defined in following equation ${ }^{(14)}$.

$$
\begin{equation*}
\sigma y\left(\varepsilon^{p}\right)=1+170\left(0.0261+\varepsilon^{p}\right)^{0.2} \quad[M P a] \tag{11}
\end{equation*}
$$

The stress of work- hardening material (copper $\sigma^{-}=430 \varepsilon^{-0.35} \mathrm{Mpa}$ ). The stress-strain curve for the work-hardening material was obtained from the simple upsetting of a cylinder made piled-up disks of annealed copper.

### 2.3 Friction Boundary Condition

If the amount and direction of the frictional shear stress are explicitly given ,the solution can be obtained simply by minimizing the functional ,equation (4).The frictional shear stress is a function of the contact pressure, location ,slipping velocity and further ,the location of the neutral point(or neutral region ).where the direction of frictional shear stress is reversed, is not known .since coulomb friction has mainly been assumed to be the frictional law of strip rolling in the aluminum industry, it will be convenient to employ the law for practical purposes. In this case, the frictional shear stress is expressed by using a coefficient of friction .the frictional shear stress is approximated by adopting the roll pressure $p$ in the previous stage of iteration in the minimizing procedure of $\Phi$. In the analysis of non-steady state rolling the nodal points are located as a new coordinates after each incremental deformation since the treatment of boundary condition is complicated if there is not anode at the corner of the roll corner of the roll entry. The element which has newly come to the entry corner is exchanged by the element with a singular point and the element which has passed through the corner is returned to the isoperimetric quadrilateral element.

## 3- FINITE ELEMENT ANALYSIS

Using ANSYS-11 the finite -element analysis was simulated by building a model same as the assumed model in theoretical analysis fig. (1). having environmental effect similar to that of reality and theoretical assumption.The model has to be meshed to a specific shape of element according to the chosen element which is solid (plane-82) with 8-node element defined by eight nodes having two degrees of freedom at each node: translations in the nodal x and y directions. The element may be used as a plane element (preferred) or as an ax symmetric element. The element has plasticity, creep, swelling, stress stiffening, large deflection, and large strain capabilities. The sharp directional change of metal flow at the corner of the roll entry is not easily represented by means of small number elements. To deal with this problem an element with a singular point which has two velocities at the corner fig. (3) is employed. Because of symmetry (about x-axis) one half of the model was first solved later the results showed by symmetry expansion of results. The loading process in ANSYS-11 is employed by applying a horizontal displacement to a work piece at time step according to the flow velocity at different load step option. The local coordinate technique was used to locally orient the axis of movement of the work piece (Aluminum) to change with the curved pass of roller. The rollers according to this technique were assumed to be fixed and squeeze the work piece into the desired thickness. The roll pressure changed from 100 to 500 Mpa with different coefficient of friction. Three models were built according to reduction of area (10, 20, and 60 percent) of the experimental work. The obtained results after applying solves
command were stress, strain shear force, shear stress and energy in both $x$ and $y$ coordinates. The shape of exit end of the strip was also obtained with the amount of change in element length before and after rolling process .the roller passed over the strip twice to have the elongation desired and agree with experimental work obtained from reference [4]

## 4- RESULTS \& DISCUSSION

Continuous rolling of a strip without front and back tension is analyzed, the process geometries and working conditions are as follows:
Roll radius: $\mathrm{R}=40 \mathrm{~mm}$
Reduction in thickness: $\mathrm{r}=10,15,20,25,30$ and $60 \%$
Initial thickness: to $=5,10,16$ and 18 mm
Coefficient of friction: $\mu f=0.03,0.1,0.3$
Flow stress (equivalent stress) $\sigma=140 e^{-0.05} \mathrm{Mpa}$
The stress strain curve was obtained by the simple compression of as received Aluminum used for rolling experiment. The plastically deforming region is assumed to be confined in the hatched region. Because the strip cannot be fed by the frictional drag forces in the early stage. The strip is pushed from the entry boundary to have a constant velocity without slip at the roll corner. When the strip begins to be driven with pushing force from the entry, the velocity boundary condition is removed.

### 4.1 Effect of Friction

Figure (4) shows the effect of friction on the ratio of plastic energy dissipation to the total energy dissipation for reduction in thickness of $r=20 \%$ and $30 \%$. WD is the rate of plastic energy dissipation which is equal to the first term on the right hand side equation -4 and W is the total rate of energy dissipation which is identical with $\phi$. In this case in the range of $\mu f<0.2$ the ratio of WD/W increases as the coefficient of friction $\mu f$ decreases because the energy dissipation due to friction loss decreases. However for a very low coefficient of friction ( $\mu f=0.04$ for $\mathrm{r}=20 \%, \mu f=0.05$ for $\mathrm{r}=30 \%$ ) the ratio is zero, the strip is not fed in to the roll gap and rolls slip over the strip, this is well agreed with numerical results obtained by using ANSYS-11 program.

### 4.2 Effect of Roll Pressure

The distribution of roll pressure for the non-hardening material in figure (5), the roll pressure shows a penning effect that is the pressure has a peak at the corner of the roll entry as observed in experiments and analysis using the slip line field method. This effect appears in the second pass (at the second load step) and the shape of the pressure distribution becomes similar to that for non-hardening material because the friction does not appear
clearly to decrease with the coefficient of friction. In general the position of the peak of the friction is quite near to that of the natural point or the center of the natural region.
Figure (6) Variation of calculated load with advancement of front end of a Aluminum strip. The peak of the roll pressure heightened as the strip advance in to the roll gap.
The calculated according to experimental shape of the tail end after rolling are compared for $\mathrm{t}_{0}=12 \mathrm{~mm}$ shows single bulging and in a good agreement with experimental one. Double bulging was obtained for to $=18 \mathrm{~mm}$. Shear force in $y$-direction when reduction of area $=30 \%$ rolling pressure equal to $300 \mathrm{Mpa} \mathrm{mf}=0.3$. The rotation angles around the TD for under the reduction of $30 \%$ are shown Since both RD rotation angles and ND rotation angles have near-zero values within the entire region they are not given in the figure. This indicates that the TD rotation also dominates for Goss initial orientation. It can be seen from that $\theta$ TD rapidly increases at the entry of the roll bite to the maximum values, and then decreases. After rolling the rotation angle around TD ( $\theta \mathrm{TD}$ ) are very small.The cases of $30 \%$ reduction increases the rotation angles around the TD, the rotation angles in the latter are much smaller than those in the former.

### 4.3 Effect of Loading

Figures (7, 8, and 9) the calculated load distribution and roll pressure for various stage of rolling of aluminum at entry and exit are shown of the front end. The velocity boundary condition that the strip is pushed from the entry boundary is assumed up the point (A) in Fig. (1) for comparison the experimentally measured load during the steady state is also illustrated, after the front end emerges from the roll gap. The load kept constant, the calculated steady state loads agree well with the experimental one and the elongation desired are agree with experimental work obtained from reference [15,16], the change due to rolling pressure changing and the velocity that the strip is flow. Figure (10,11).The effect of friction coefficient on the ratio of plastic energy dissipation to the total energy.

The strip rolling processes with a constant coefficient of friction under plane - strain condition were successfully calculated with the present method is effective by obtaining precise contact pressure distribution and in predicting the non-uniform deformation of the front end tail ends. The roll pressure during the steady state exhibits two peaks at the neutral point or region and the roll entry, in the case of non-hardening material and the second pass of material, whereas the peak at the roll entry is not observed in the first pass of material.

In steady state rolling, the strip is not driven in to the roll gap when the coefficient of friction is very small when ( $\mu f=0.04$ for $\mathrm{r}=20 \%, \mu f=0.05$ for $\mathrm{r}=30 \%$ ) the front end of the rolled strip shows a double bulge (when taking full model) and the tail end a single or double bulge. The calculated Result after rolling agrees well with the experimental as show in
figures $(12,13)$ and the element consists of triangular sub element igm and quadrilateral ijkim shown in figure (2) the boundary condition at the corner is well satisfied.

## 5. CONCLUSIONS

The rigid-plastic finite element method was applied to the analysis of steady and non-steady state rolling. The steady and non-steady state strip rolling processes with a constant coefficient of friction under plane-strain condition were successfully simulated .In general the present method is effective is obtaining precise contact pressure distribution and in predicting the non-uniform deformation of the front and tail ends. The results of the present analysis are summarized as follows ;

1) The roll pressure during the steady state exhibits two peaks at the neutral point or region and the roll entry in the case of non-hardening material and the second pass of workhardening material whereas the peak at the roll entry is not observed in the first pass of work-hardening material.
2) In steady state rolling the strip is not driven into the roll gap when the coefficient of friction is very small e.g. $\mu<0.04$ for $\mathrm{r}=20 \%$ and $\mu<0.05$ for $\mathrm{r}=30 \%$.
3) The front end of the rolled strip shows a double bulge and the tail end a single or double bulge. The calculated end shapes agree well with the experimental ones.

## REFERENCES:

1- Tamano .T \& Anagimoto. S. Y. "Finite Element Analysis of Steady Metal Flow Problems" Trans JSME 41, 1130 [1985].
2- Dawson .P.R and Thompson. E. G. "Finite Element Analysis of Steady State ElastioVisco Flow by The Initial Stress Rate Method" J .Num .Mech. Eng.12, 47 [1987].
3- Ona. H. \& Jimma. T "Prevention of Shape Defects in the Cold - Roll Forming Process of Wide Profiles" Bulletin of Precision Machinery and Electronics, Tokyo Institute of Technology No. 53 pp 1-13 [1994].
4- Dobrev A \& Halmos G. T. "Roll Design Charlotte .NC. FMAS" Roll Forming Process Conference [1997].
5- Dong. C. "Deformation Mechanics in Cold - Roll Formed Wide Profiles" M.S. Project. University of Pittsburgh [1998].
6- Collins. I. F. "Slip Line Field Solution For Compression And Rolling With Slipping Friction" Int. J. Mech. Sic 11, [1997].
7- Vizur. B "An Upper-Bound Approach to Cold Strip Rolling" J. Eng. Indust. Trans ASME68-31 [1998].

8- Rao. S and Kumar. K "Finite Element Analysis of Cold Strip Rolling" Int. J Mech Tool Design. (1998).
9- Mori .K "Simulation of Plane Strain Rolling by the Rigid Plastic finite Element Method" Int. J. Mech. Sci. Vol. 24, No. 9 pp $519-527,1982$
10- Shima S. and Mori K. "Rigid Plastic Finite Element Analysis of Strip Rolling" proc $4^{\text {th }}$ Int. Conf. Prod. Eng. Tokuo p 80 [1992].

11-Osak. K and Nakano .J "Finite Element Method for Rigid Plastic Analysis of Metal Forming Formulation" Int. J. Mech. Sci. 24, 459 [1998].

12- Alexander Kainz "Finite Element Modeling of Temper Rolling with Particular Emphasis on Roughness Transfer" ABAQUS Austria users conference vol. 27/28 pp1-10 September. [2005].
13- Tarnopolskaya Tand. Gates .D. J "Numerical Analysis of Lateral Movement of A metal Strip during Cold Rolling" ANZIM .J 45 pp 173-186 [2004].

14-Stefqnik A "Slitting Criterion for Various Rolling Speeding in MSR Rolling Process" AMME Journal of achievements in materials and manufacturing engineering vol. 27 pp . 94-104 [2008].

15- Oladipo. Jr. Onipede "Simulation of Cold Roll Forming of Steel Panels" Mechanical Engineering Department, University of Pitsburgh. Benedum Engineering Hall 3700 Q. Hara Street office 648 USA [2008].
16-Klaus Hulka "The Role of Niobium in Low Carbon Bainitic Hsla Steel" Niobium Products Company Gmbh, Dusseldorf, Germany [2009].

Table (1): Geometric Properties Model for Steady State Rolling used in this research.

| Main Roller Diameter | 400 mm |  |  |
| :---: | :---: | :---: | :---: |
| Velocity of the Plate | $1500 \mathrm{~mm} / \mathrm{sec}$ |  |  |
| Dimension of the Plate | $1500 \times 500 \times 5 \mathrm{~mm}$ |  |  |
|  | Case 1 | Case 2 | Case 3 |
| Center to Center Distance | 300 mm | 300 mm | 300 mm |
| Displacement of Bottom Roller <br> Applied | 90 mm | 90 mm | 90.01 mm |
| Static Dynamic Friction | $0 / 0$ | $0 / 0$ | $0.02 / 0.01$ |
| Coefficient of friction $\mu$ | 0.03 | 0.1 | 0.3 |
| Initial thickness to $=5,10,16,18, \mathrm{~mm}$ |  |  |  |
| Reduction in thickness <br> $\mathrm{r}=8,10,20,30,40,50 \%$ |  |  |  |



Figure (1): General idea of Modeling of Plane -Strain Rolling


Figure (2): Treatment of Velocity Boundary Condition at Corner or Roll Entry
(a) Triangular sub- element ijm and quadrilateral sub - element ijkm
(b) Element with a singular


Figure (3): Steady State Geometry Mesh Symmetry.


Figure (4): Nodal Elastic Strain Distribution when Rolling Pressure $=300 \mathrm{Mpa}$ and $\mu_{\mathrm{f}}=0.3$


Figure (5): X-Displacement (flow direction) with Rolling Pressure $=300$ Map, $\mu_{\mathrm{f}}=0.3$ and Reduction of Area $=40 \%$


Figure (6): Shear Force in y-direction when Reduction of Area $=30 \%$ Rolling Pressure equal to 300 Mpa and $\mu_{\mathrm{f}}=0.3$


Figure (7): Shape Change of Front End of an Aluminum Strip according to Loading Step and Rolling Pressure.


Figure (8): Calculated Distribution of Roll Pressure for Various Stage of Rolling of
Aluminum at Entry and Exit


Figure (9): Variation of Calculated Load with advancement of Aluminum Strip when $\mu_{\mathrm{f}}=0.15,0.25$ at Entry and Exit


Figure (10): The effect of friction coefficient on the ratio of plastic energy Dissipation to the total energy


Figure (11): The Average Effective Strain with different Contact Surfaces Between Aluminum and Rollers with Variation Friction Factor


Figure (12): External Load and Displacement curves Comparison between calculated and experimental (no lubrication) after rolling for to $=12 \mathrm{~mm}, m f=0.25,{ }^{(9)}$


Figure (13): Distributions of radial strain on initial radius when the external load equal 800 kg comparison of theory result, F.E.M and Experimental.

# تحليل الانفعال المستوي لعملية الارفلة لمادة صلبة لانة باستخدام طريقة العناصر 

## المحددة

سعد ذياب فارس
استاذ مساعد، كلية الينسسة، جامعة ديالى


#### Abstract

الخلاصة: فى هذا البحث تم استخدام مادة صلبة للنة لحالة الاستقرارية وعدم الاستقرارية للارفلة الانزلاقية وبتوزيع الانفعالات والاجهادات في حالة الاستقرار تحت ظروف الاحتكاك الثابت وحسابها بوجود التصليد واللاتصليدالانفعالي للمادة. وتم بناء نظام دقيق للليطرة على عطية الاستطالة عند الارفلة للتتبؤ بالضغط، السرعة والانزلاق للامام للحصول على ادق وصف لما يحدث فى الطبقات التحتية للصفيحة المدرفلة.استخدم تقريب عددى لمعرفة دقة وتتظيم الموديلات التحليلية باستخدام التحليل اللاخطى فى برنامج (Ansys-11) بالاعتماد على طريقة العناصر المحددة. استغل التمانل و النققد فى معرفة الاجهاد والانفعال فى الحالة المستقرة للارفلة ثنائية الابعاد فى حالة كون معامل الامل الاحتكاك ثابت للمعادن غير الصصلدة. تم بناء موديل تحليلي وامكن تحديده في مقدار التخصر في المساحة طبقا الى قطر الدرفيل، المسافة بين الارفيل وضغط الدرفيل للحصول على انسب تصميم لعملية الدرفلة للالمنيوم. تم حساب ضغط الارفلة الناشئ وكان ذروته في مقدمة الاخول للارفيل والذي لم يظهر بطريقة النسطيح اما الاوران حول اتجاه الارفيل والاتجاه الطبيعي اهطل واتجاه انتقال زاوية الدوران يزداد بزيادة التخصروانه لعب دورمهمها في تقويم الارفلة. شكل الصفيحة بعد الارفلة ومقدار استطالة العناصر امكن تحديده مع عدة منحنيات بحيث قورنت الموديلات التحليلية المخنلفة فى مقار النقليل فى المساحة مع الننائج العملية للحصول على انسب تصميم لعملية الارفلة للالمنيوم ولتحسين نوعية المنتج والسيطرة على الدرفلة الانتاجية مع اعطاء وصف نهائى لعطلية الدرفلة ولكون عملية الارفلة تحدث تنيير فليل فى السمك تتحدد نقطة الخضوع للاستطالة مع التركيز على العناصر السطحية التى تتعرض الى اجهاد انضغاطى وتنتويه دائم يزداد بزيادة التخصر • زاوية الدوران لنموذج الدرفلة صغيرة جدا وهذه النتائج للشكل النهائي كانت متوافقة بشكل جيد مع النتائج العطلية للالمنيوم.


